

## Focusing light through scattering media by full-polarization digital optical phase conjugation

YUECHENG SHEN,<sup>†</sup> YAN LIU,<sup>†</sup> CHENG MA, AND LIHONG V. WANG<sup>\*</sup>

Optical Imaging Laboratory, Department of Biomedical Engineering, Washington University in St. Louis, One Brookings Drive, St. Louis, Missouri 63130, USA

<sup>\*</sup>Corresponding author: lhwang@wustl.edu

Received 3 November 2015; revised 13 January 2016; accepted 17 January 2016; posted 19 January 2016 (Doc. ID 253100); published 8 March 2016

**Digital optical phase conjugation (DOPC) is an emerging technique for focusing light through or within scattering media such as biological tissue. Since DOPC systems are based on time reversal, they benefit from collecting as much information about the scattered light as possible. However, existing DOPC techniques record and subsequently phase-conjugate the scattered light in only a single-polarization state, limited by the operating principle of spatial light modulators. Here, we develop the first, to the best of our knowledge, full-polarization DOPC system that records and phase-conjugates scattered light along two orthogonal polarizations. When focusing light through thick scattering media, such as 2 mm and 4 mm-thick chicken breast tissue, our full-polarization DOPC system on average doubles the focal peak-to-background ratio achieved by single-polarization DOPC systems and improves the phase-conjugation fidelity.** © 2016 Optical Society of America

**OCIS codes:** (110.0113) Imaging through turbid media; (170.7050) Turbid media; (110.1080) Active or adaptive optics; (070.5040) Phase conjugation; (290.5855) Scattering, polarization.

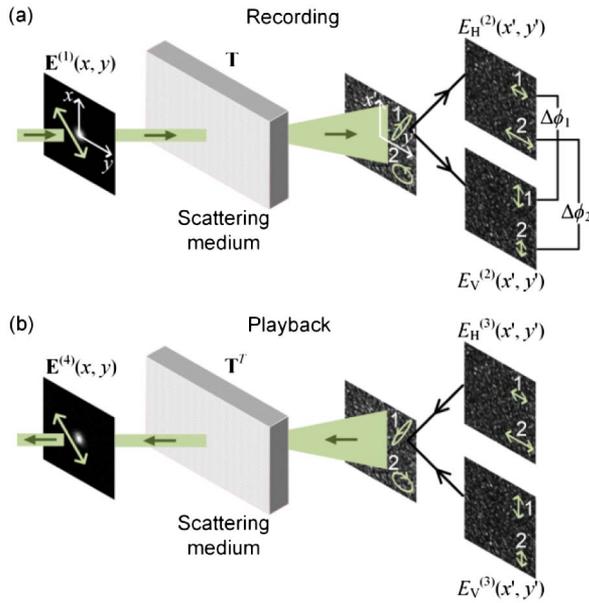
<http://dx.doi.org/10.1364/OL.41.001130>

Focusing light through or within scattering media is critically important in many applications, such as high-resolution optical imaging, photodynamic therapy, and optical manipulation. However, in scattering media such as biological tissue, light gradually loses the memory of its initial propagation direction due to scattering, which makes it difficult to create a focus beyond the optical diffusion limit ( $\sim 1$  mm deep) [1–3]. To break this fundamental limit, various methods have been developed, including iterative wavefront shaping [4–6], transmission matrix measurement [7], and optical phase conjugation (OPC) [8–21]. Among all these approaches, OPC, which is based on the principle of time reversal, determines the optimum wavefront without time-consuming iterations. There are two categories of OPC: analog OPC [8–11], based on nonlinear crystals, and digital OPC (DOPC) [12–21], based on electronic cameras and spatial light modulators (SLMs). Compared with analog OPC, DOPC has several advantages. First, unlike

analog OPC systems, which work with a narrow wavelength range dictated by the properties of the nonlinear crystals, the specific wavelength used by DOPC systems can be tuned in a relatively large range without modifying the system. Second, DOPC has much higher phase conjugation reflectivity. Third, DOPC supports playback of a synthesized field, not just a directly recorded OPC field [18–21].

When the scattering medium is optically thick, the polarization of the scattered light becomes spatially randomized. Thus, in any OPC experiment, it is ideal to first record all the information about the scattered light, including its phase, amplitude, and polarization at all positions. Next, to follow the time-reversal principle rigorously, scattered light needs to be phase-conjugated with the original position-dependent polarizations maintained. Using a nonlinear crystal, a full-polarization analog OPC system has been developed to restore images through multimode fibers [9]. However, in practice, the SLMs used in DOPC systems can modulate only linearly polarized light along a fixed direction, and thus are incapable of faithfully phase-conjugating scattered light with different polarization states. To address this problem, we have developed the first full-polarization DOPC system that is able to record and phase-conjugate light with random polarizations.

The process of full-polarization DOPC includes a recording step and a playback step (Fig. 1). In the recording step [Fig. 1(a)], the incident light  $\mathbf{E}^{(1)}(x, y)$  passes through a scattering medium and evolves into a fully developed speckle pattern on the  $x' - y'$  plane, with spatially nonuniform polarizations. In order to record the information about scattered light with various polarizations, the scattered light is decomposed into two components:  $E_H^{(2)}(x', y')$  and  $E_V^{(2)}(x', y')$ , and both are recorded using phase-shifting holography [22]. In general, the speckle patterns corresponding to the two orthogonal polarizations bear little resemblance, and the polarizations at two arbitrary positions that are not within the same speckle grain, i.e., position 1 and position 2 [Fig. 1(a)], are completely uncorrelated in both amplitude ratio and relative phase. Next, in the playback step [Fig. 1(b)], both OPC fields, with orthogonal polarizations, are produced and directed to the scattering medium. After they pass through the scattering medium, an output collimated beam that is phase-conjugated to the input beam is obtained.



**Fig. 1.** Schematic of the processes in full-polarization DOPC. (a) In the recording step, the scattered light is recorded along the horizontal (H) and vertical (V) polarizations. (b) In the playback step, OPC fields along the two orthogonal polarizations are produced and become phase-conjugated to the input light field after passing through the scattering medium.

We theoretically studied full-polarization DOPC by extending the existing scalar-field-based random matrix theory [23]. The input light field  $\mathbf{E}^{(1)}(x, y)$  is expressed as a Jones column vector concatenated by two components  $E_H^{(1)}(x, y)$  and  $E_V^{(1)}(x, y)$ :

$$\mathbf{E}^{(1)}(x, y) = \begin{pmatrix} E_H^{(1)}(x, y) \\ E_V^{(1)}(x, y) \end{pmatrix}_{2N \times 1}, \quad (1)$$

where each component comprises  $N$  spatial modes and is represented by an  $N \times 1$  column vector. Since light transmission through the scattering medium and the subsequent optics is represented by a vector transmission matrix  $\mathbf{T}$  [24,25], the scattered light field on the SLM  $\mathbf{E}^{(2)}(x', y') = \begin{pmatrix} E_H^{(2)}(x', y') \\ E_V^{(2)}(x', y') \end{pmatrix}_{2N \times 1}$  can be calculated as  $\mathbf{E}^{(2)}(x', y') = \mathbf{T}\mathbf{E}^{(1)}(x, y)$ . Specifically, the vector transmission matrix has the following form:

$$\mathbf{T} = \begin{pmatrix} \mathbf{T}_{HH} & \mathbf{T}_{HV} \\ \mathbf{T}_{VH} & \mathbf{T}_{VV} \end{pmatrix}_{2N \times 2N}, \quad (2)$$

in which  $\mathbf{T}_{AB}$  ( $A, B = H, V$ ) is an  $N$ -by- $N$  matrix that connects the input field with  $B$  polarization and the scattered field with  $A$  polarization. By using singular value decomposition, each  $\mathbf{T}_{AB}$  can be further decomposed as  $\mathbf{T}_{AB} = \mathbf{U}_{AB}\mathbf{t}_{AB}\mathbf{V}_{AB}$ , where  $\mathbf{U}_{AB}$  and  $\mathbf{V}_{AB}$  are independent unitary matrices. Physically,  $\mathbf{U}_{AB}$  and  $\mathbf{V}_{AB}$  are transformation matrices converting between coordinates in Cartesian bases and eigenmode bases.  $\mathbf{t}_{AB}$  is a diagonal matrix with nonnegative elements, and each element quantifies the transmission coefficient of each eigenmode. Thus,  $\tau_{AB} = \text{tr}(\mathbf{t}_{AB}^2)/N$  represents the average power transmission from polarization  $B$  to polarization  $A$ , where  $\text{tr}(\cdot)$  denotes taking the trace of a matrix. In practice, only a fraction of the transmitted light is measured. Under this condition, the elements in each  $\mathbf{T}_{AB}$  can be approximated by the corresponding circular Gaussian distributions [23]. Thus, for scattering media that are sufficiently

thick to randomize the polarization state,  $\mathbf{T}_{AB}\mathbf{T}_{AB}^\dagger \approx \tau_{AB}\mathbf{I}$ , where the symbol  $\dagger$  represents the adjoint of a matrix and  $\mathbf{I}$  is an identity matrix. The playback OPC field is phase-conjugated to the recorded field:  $\mathbf{E}^{(3)}(x', y') = [\mathbf{E}^{(2)}(x', y')]^*$ , where the symbol  $*$  denotes complex conjugation. Finally, the output field  $\mathbf{E}^{(4)}(x, y) = \begin{pmatrix} E_H^{(4)}(x, y) \\ E_V^{(4)}(x, y) \end{pmatrix}$  after scattering is estimated by  $\mathbf{E}^{(4)}(x, y) = \mathbf{T}^T\mathbf{E}^{(3)}(x', y')$ , where the scattering matrix is modeled by the transpose of the forward transmission matrix. Thus,

$$\mathbf{E}^{(4)}(x, y) \approx \begin{pmatrix} (\tau_{HH} + \tau_{VH})[E_H^{(1)}(x, y)]^* \\ (\tau_{HV} + \tau_{VV})[E_V^{(1)}(x, y)]^* \end{pmatrix} + \begin{pmatrix} (\mathbf{M}_{VHH} + \mathbf{M}_{V VH})[E_V^{(1)}(x, y)]^* \\ (\mathbf{M}_{HHV} + \mathbf{M}_{HVV})[E_H^{(1)}(x, y)]^* \end{pmatrix}. \quad (3)$$

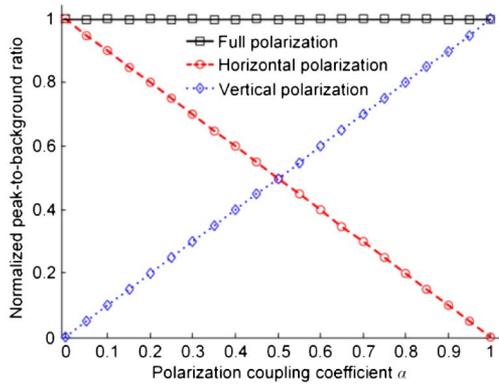
Here, the first term on the right-hand side of Eq. (3) represents the phase-conjugated light, and the second term represents a background due to polarization coupling in partial OPC. Specifically, matrices  $\mathbf{M}_{ABC} \equiv \mathbf{T}_{BC}^T\mathbf{T}_{BA}^*$  with  $A, B, C = H, V$  and  $A \neq C$  describe the mapping from the input light with  $A$  polarization to the scattered light with  $B$  polarization, followed by the mapping from the scattered light with  $B$  polarization to the output light with  $C$  polarization. The modulus of each element in  $\mathbf{M}_{ABC}$  is  $O(1/N^{1/2})$ . Physically,  $(\tau_{HH} + \tau_{VH})$  and  $(\tau_{HV} + \tau_{VV})$  are the total transmittances of the scattering medium when the incident light is purely horizontally polarized or purely vertically polarized, respectively. For most scattering media, these two values are very close. Therefore,  $\mathbf{E}^{(4)}(x, y) \approx \beta\mathbf{E}^{(1)}(x, y)^*$ , where  $\beta = (\tau_{HH} + \tau_{VH})$  [or  $(\tau_{HV} + \tau_{VV})$ ] is a positive number. So, the full-polarization DOPC process faithfully produces the phase-conjugated field of the input light. However, if the DOPC process phase-conjugates scattered light only along the horizontal polarization direction (referred to as single-polarization DOPC), the output field is calculated as

$$\mathbf{E}^{(4)}(x, y)|_H \approx \begin{pmatrix} \tau_{HH}[E_H^{(1)}(x, y)]^* \\ \tau_{HV}[E_V^{(1)}(x, y)]^* \end{pmatrix} + \begin{pmatrix} \mathbf{M}_{VHH}[E_V^{(1)}(x, y)]^* \\ \mathbf{M}_{HHV}[E_H^{(1)}(x, y)]^* \end{pmatrix}. \quad (4)$$

In cases when  $\tau_{HH}$  and  $\tau_{HV}$  are not the same, the resultant field is not phase-conjugated to the input light field.

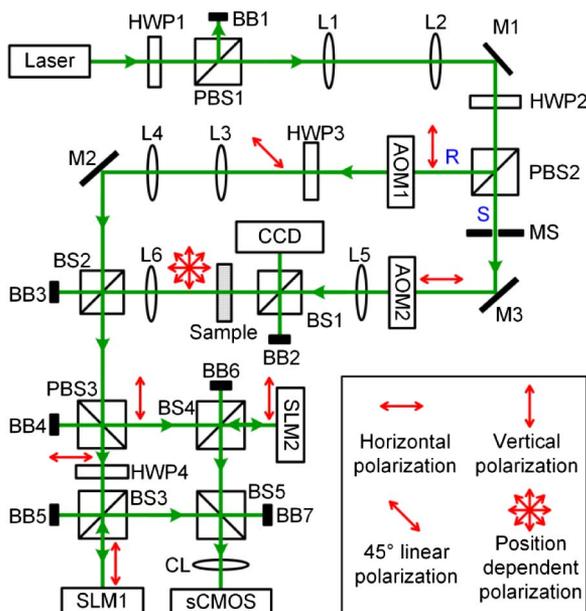
To compare the performance of full-polarization DOPC and single-polarization DOPC we performed numerical simulations, and the input light was chosen to be horizontally polarized with the central pixel being 1 for the electric field amplitude and the other pixels being 0. Each element in the transmission matrix  $\mathbf{T}_{AB}$  was drawn from a circular Gaussian distribution with mean  $\mu = 0$  and variance  $\sigma^2 = \tau_{AB}$ . Specifically,  $\tau_{HH}$  was varied from 0 to 1, and we assumed  $\tau_{VV} = \tau_{HH}$  and  $\tau_{HV} = \tau_{VH} = 1 - \tau_{HH}$ . Figure 2 plots the peak-to-background ratio (PBR) normalized by  $N$  ( $=2500$ ) as a function of the polarization-coupling coefficient  $\alpha$ . PBR is defined as the ratio between the average intensities within and outside the targeted region of the phase-conjugated light;  $\alpha$  quantifies the average energy transfer between the two orthogonal polarizations, and is defined as  $\alpha \equiv \tau_{VH}/(\tau_{HH} + \tau_{VH})$ .

Figure 2 shows that the normalized PBRs for full-polarization DOPC are 1 for all values of  $\alpha$ . In contrast, the normalized PBRs for single-polarization DOPC change linearly with  $\alpha$ . Such an observation is in accord with the theoretical expression of the normalized PBRs for single-polarization



**Fig. 2.** Normalized PBR as a function of the polarization coupling coefficient  $\alpha$  for three different DOPC schemes. Discrete data points are from numerical simulation results, while the lines are plotted using analytical expressions.

DOPC ( $= 1 - \alpha$  and  $\alpha$  for horizontal and vertical polarization DOPC respectively, which can be derived by following the same procedures in [23] but using the vector transmission matrix). Specifically, when  $\alpha$  approaches 0.5, the PBRs achieved by horizontal-polarization DOPC and vertical-polarization DOPC are the same, and they are half of the PBR achieved by full-polarization DOPC. An intuitive explanation is that in the full-polarization scenario, the peak intensity is enhanced by a factor of 4 due to constructive interference, while the background is doubled by summing the background intensities corresponding to the two orthogonal polarizations. When  $\alpha$  approaches 0 or 1, if the correct polarization state is not chosen



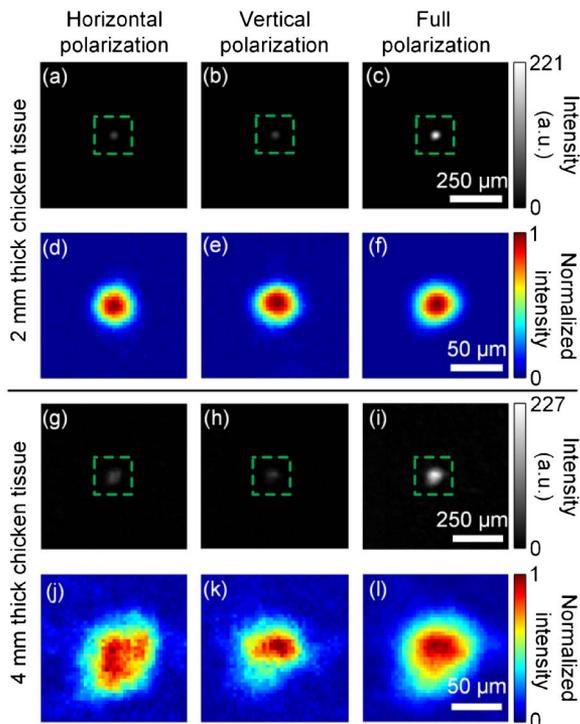
**Fig. 3.** Schematic of the full-polarization DOPC setup. Polarization states are indicated by the red arrows. AOM: acousto-optic modulator; BB: beam block; BS: beam splitter; CCD: CCD camera; CL: camera lens; HWP: half wave plate; L: lens; Laser: Verdi V5, Coherent, 532 nm; M: mirror; MS: mechanical shutter; PBS: polarizing beam splitter; R: reference beam; S: sample beam; sCMOS: scientific CMOS camera (pco.edge 5.5); SLM: spatial light modulator (Pluto NIR-II, Holoeye).

to record and phase-conjugate the scattered light, the PBR of single-polarization DOPC can become extremely low. In practice,  $\alpha \sim 1$  corresponds to a strongly birefringent sample with a small optical thickness, such as the retina of the eye [26]. Based on the above analysis, it is highly desirable to develop a full-polarization DOPC system. The performance of such a system is not sensitive to the properties of the scattering media, and the system can always achieve a higher PBR than that achieved by single-polarization DOPC systems.

Then, we developed a full-polarization DOPC system, schematically shown in Fig. 3. In the phase recording step, the input light was split into a planar reference beam (R) and a sample beam (S) by a polarizing beam splitter (PBS). Each beam was subsequently modulated by an acousto-optic modulator to induce a 12 Hz frequency difference between R and S. The polarization direction of R was then rotated by a half wave plate (HWP) to 45 degrees. In the sample arm, S illuminated an *ex vivo* chicken breast tissue slice, and its polarization state became spatially inhomogeneous after tissue scattering. Then, the two beams were combined by a 50:50 beam splitter (BS) for interferometry. Since the scattered light took various polarization states, we used a PBS to separate it spatially into components with horizontal and vertical polarizations. Each component then impinged on the surface of an SLM. Both SLMs had a resolution of 1920 pixels  $\times$  1080 pixels, and were imaged onto a camera (resolution 2560 pixels  $\times$  2160 pixels). Each pixel in the SLMs corresponded to one pixel on the camera. The phase maps corresponding to the horizontally polarized scattered light and the vertically polarized scattered light were measured using phase-shifting holography [17,22], made possible by making the camera run at a frame rate of 48 Hz ( $= 4 \times 12$  Hz).

In the playback step, the conjugate phase maps were displayed on the respective SLMs. An experimentally determined constant phase offset was added to one of the phase maps to compensate for the path length difference. The sample beam was blocked and the planar reference beam illuminated the two SLMs to acquire the conjugate phase map. The two branches of phase-conjugated light were then combined by PBS3 and were directed to the scattering sample. After they passed through the sample, a bright focus was formed on the focal plane of lens L5. A 10:90 BS was inserted to create a copy of the focus, which was captured by a CCD camera.

In our experiment, we used 2 mm and 4 mm thick chicken breast tissue as scattering samples, and  $\alpha$  was close to 0.5 for both samples, which is expected for thick scattering media. Figures 4(a)–4(c) show the imaged foci when only horizontal polarization, only vertical polarization, and full polarization were used for DOPC through 2 mm thick chicken breast tissue. All three images are shown using the same intensity scale. The peak intensity of the focus achieved by full-polarization DOPC is approximately four times as high as that achieved by single-polarization DOPC. Moreover, the PBRs for the three images are 141, 135, and 262, respectively. This result illustrates that the PBR achieved by full-polarization DOPC is roughly twice that achieved by single-polarization DOPC, which is in good agreement with our theoretical predictions. To better visualize the shape of the focus, each image is zoomed in and is normalized by its own peak intensity, as shown in Figs. 4(d)–4(f). It can be seen that all three foci maintain nearly circular shapes, which shows that when the sample is not too thick, single-polarization DOPC can still achieve high OPC



**Fig. 4.** Images of the foci achieved by single-polarization and full-polarization DOPC. (a)-(c) Images of the foci through 2 mm thick chicken breast tissue when only horizontal-polarization, only vertical-polarization, and full-polarization DOPC were employed. (d)-(f) Enlarged images of (a)-(c). To better visualize the shape of the focus, each image is normalized by its own peak intensity. (g)-(i) Images of the foci through 4 mm thick chicken breast tissue (j)-(l) Enlarged images of (g)-(i) with renormalization.

fidelity. For the 4 mm thick chicken tissue, the images of the foci achieved by horizontal-polarization, vertical-polarization, and full-polarization DOPC are shown in Figs. 4(g)–4(i), respectively. Again, the intensity of the focus achieved by full-polarization DOPC is roughly four times as high as that achieved by single-polarization DOPC. The PBRs for the three images are calculated to be 21, 18, and 37. Thus, full-polarization DOPC still approximately doubles the PBR achieved by single-polarization DOPC. Figures 4(j)–4(l) show the enlarged images of the foci after normalization by their own peak intensities. Among all three foci, the one achieved by full-polarization DOPC has a nearly circular shape that most closely resembles the shape of the input focus. Such a result indicates that when the sample is thick, full-polarization DOPC can achieve higher OPC fidelity than that achieved by single-polarization DOPC [9]. We note that the increased size of the foci for 4 mm thick chicken tissue is due to different experimental conditions.

Here, we briefly discuss the polarization states of the OPC field in our experiments. Currently, the two SLMs in the setup modulate only the phase, but not the amplitude of light. Thus, the SLM-generated OPC field before illuminating the sample does not have the same polarization as that of the scattered light. Nonetheless, compared with the ideal case when both phase and amplitude are modulated due to the scrambling nature of the thick scattering medium, the phase-modulated light still constructively interferes in the same polarization state as that of

the recording-phase input light (though the amplitude is reduced), while there is no constructive interference in the orthogonal polarization state. Thus, after the SLM-generated OPC field passes through the scattering medium, the polarization of the electric field at the focus is approximately the same as that of the input field. In our experiments, the input electric field at the focus was set to be horizontally polarized. Using a polarizer, we confirmed that the electric field at the focus achieved by full-polarization DOPC was also horizontally polarized.

In conclusion, we have developed the first DOPC system that can record and phase-conjugate the scattered light with various polarization states. When the scattering sample is optically thick, our system doubles the PBR achieved by single-polarization DOPC systems, improves the OPC fidelity, and maintains the polarization of the input light field. The method described here can be easily applied to existing DOPC systems to improve their performance.

**Funding.** National Institute of Health (DP1 EB016986), (R01 CA186567).

**Acknowledgment.** We thank Jinyang Liang for helpful discussions, and James Ballard for proofreading the manuscript.

<sup>†</sup>These authors contributed equally to this work.

## REFERENCES

- V. Ntziachristos, *Nat. Methods* **7**, 603 (2010).
- Y. Liu, C. Zhang, and L. V. Wang, *J. Biomed. Opt.* **17**, 126014 (2012).
- L. V. Wang and H. Wu, *Biomedical Optics: Principles and Imaging* (Wiley, 2007).
- I. M. Vellekoop and A. P. Mosk, *Opt. Lett.* **32**, 2309 (2007).
- M. Cui, *Opt. Express* **19**, 2989 (2011).
- P. Lai, L. Wang, J. W. Tay, and L. V. Wang, *Nat. Photonics* **9**, 126 (2015).
- S. Popoff, G. Lerosey, R. Carminati, M. Fink, A. Boccarda, and S. Gigan, *Phys. Rev. Lett.* **104**, 100601 (2010).
- Z. Yaqoob, D. Psaltis, M. S. Feld, and C. Yang, *Nat. Photonics* **2**, 110 (2008).
- P. H. Beckwith, I. McMichael, and P. Yeh, *Opt. Lett.* **12**, 510 (1987).
- X. Xu, H. Liu, and L. V. Wang, *Nat. Photonics* **5**, 154 (2011).
- Y. Liu, P. Lai, C. Ma, X. Xu, A. A. Grabar, and L. V. Wang, *Nat. Commun.* **6**, 5904 (2015).
- M. Cui and C. Yang, *Opt. Express* **18**, 3444 (2010).
- C.-L. Hsieh, Y. Pu, R. Grange, G. Laporte, and D. Psaltis, *Opt. Express* **18**, 20723 (2010).
- T. R. Hillman, T. Yamauchi, W. Choi, R. R. Dasari, M. S. Feld, Y. Park, and Z. Yaqoob, *Sci. Rep.* **3**, 1909 (2013).
- D. Wang, E. H. Zhou, J. Brake, H. Ruan, M. Jang, and C. Yang, *Optica* **2**, 728 (2015).
- Y. M. Wang, B. Judkewitz, C. A. DiMarzio, and C. Yang, *Nat. Commun.* **3**, 928 (2012).
- K. Si, R. Fiolka, and M. Cui, *Nat. Photonics* **6**, 657 (2012).
- B. Judkewitz, Y. M. Wang, R. Horstmeyer, A. Mathy, and C. Yang, *Nat. Photonics* **7**, 300 (2013).
- C. Ma, X. Xu, Y. Liu, and L. V. Wang, *Nat. Photonics* **8**, 931 (2014).
- E. H. Zhou, H. Ruan, C. Yang, and B. Judkewitz, *Optica* **1**, 227 (2014).
- C. Ma, F. Zhou, Y. Liu, and L. V. Wang, *Optica* **2**, 869 (2015).
- I. Yamaguchi and T. Zhang, *Opt. Lett.* **22**, 1268 (1997).
- I. M. Vellekoop, "Controlling the propagation of light in disordered scattering media," Ph.D. dissertation (University of Twente, 2008).
- S. Tripathi, R. Paxman, T. Bifano, and K. C. Toussaint, *Opt. Express* **20**, 16067 (2012).
- J. Park, J.-H. Park, H. Yu, and Y. Park, *Opt. Lett.* **40**, 1667 (2015).
- B. Cense, T. C. Chen, B. H. Park, M. C. Pierce, and J. F. de Boer, *Invest. Ophthalmol. Visual Sci.* **45**, 2606 (2004).